

Neo-darwinian evolution implies punctuated equilibria

C. M. Newman*, J. E. Cohen†§ & C. Kipnis‡

* Department of Mathematics, University of Arizona, Tucson, Arizona 85721, USA

† Laboratory of Populations, Rockefeller University, New York, New York 10021-6399, USA

‡ Centre de Mathématiques appliquées, Ecole Polytechnique, Palaiseau 91128, France

The two central elements of neo-darwinian evolution^{1,2} are small random variations and natural selection. In Wright's view, these lead to random drift of mean population characters in a fixed, multiply peaked 'adaptive landscape', with long periods spent near fitness peaks^{3,4}. Using recent theoretical results⁵, we show here that transitions between peaks are rapid and unidirectional even though (indeed, because) random variations are small and transitions initially require movement against selection. Thus, punctuated equilibrium^{6,7}, the palaeontological pattern^{8,9} of rapid transitions between morphological equilibria, is a natural manifestation of the standard wrightian evolutionary theory and requires no special developmental, genetic or ecological mechanisms¹⁰⁻¹³.

The simplest neo-darwinian model for the evolution of the population mean \bar{x} of a genetically determined character expresses the change $d\bar{x}$ in time interval dt as the sum of a natural selection term and a random variation term:

$$d\bar{x}(t) = F'(\bar{x}(t)) + \alpha dW(t) \quad (1)$$

$F(\bar{x})$, a one-dimensional genotypic³ or phenotypic¹⁴ adaptive landscape, describes the mean population fitness. If, for example, the slope F' is positive (a rising landscape) at $\bar{x}(t)$, natural selection pushes \bar{x} towards larger values. The parameter α gives the magnitude of random variations relative to that of natural selection. The random process $W(t)$, a standard brownian movement with zero mean drift, represents, for example, genetic drift and short-term environmental fluctuations showing no obvious trend. We assume, for simplicity, that α is independent of \bar{x} .

Suppose that the landscape is doubly peaked: as \bar{x} increases, F rises to a peak at $\bar{x} = p$, declines to a valley at $\bar{x} = v$, rises to a second higher peak at $\bar{x} = P$, then declines. Let the initial value $\bar{x}(0)$ be smaller than v . To mimic the fossil record, suppose $\bar{x}(t)$ is observed, not continuously, but at some finite (perhaps large) number N of epochs $0 < t_1 < \dots < t_N$, perhaps chosen by another random process modelling stratigraphic sampling. There is a natural timescale τ_α associated with transitions from the smaller to the larger peak which increases dramatically as α decreases. We suppose that the intervals between observations are, for small values of α , proportional to τ_α .

Under these assumptions⁵, for small α , the observed $\bar{x}(t_i)$ values behave quite differently from $\bar{x}(t)$ itself, which is intrinsically continuous. As α approaches 0, the observed values become fixed exactly at p for some random (exponentially distributed) time, then jump (apparently) instantaneously to P and remain there (apparently) indefinitely. Analogous results hold if F has more than two peaks⁵ or if \bar{x} is multidimensional¹⁵.

To understand this result, note that a movement of \bar{x} from p to v goes against the influence of natural selection and, for small α , is very improbable. Improbable events eventually occur (with timescale τ_α) and then by the most likely of the improbable alternatives. Here it is most likely⁵ that small random variations combine to push \bar{x} from p to v as if the direction of natural selection were reversed, hence rapidly and unidirectionally. Once at v , the move to P is by natural selection. The rapidity of the second part of the transition is well recognized⁴, whereas

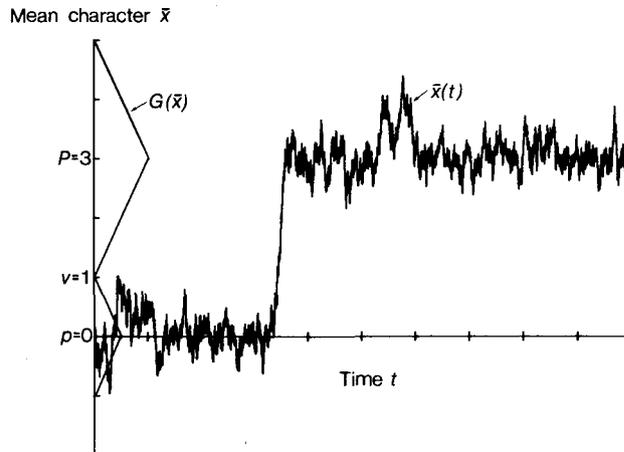


Fig. 1 Punctuated equilibria in a numerical solution of the discrete time equation, $\bar{x}(t+1) - \bar{x}(t) = G'(\bar{x}(t)) + s w_t$. The landscape G has a lower peak at $\bar{x} = 0$, a valley at $\bar{x} = 1$ and a higher peak at $\bar{x} = 3$; its slope, G' , takes only the values $+0.01$ or -0.01 . w_t Represents the sign of random variables, s their magnitude. For each t , w_t is independently $+1$ or -1 with equal probability; $s = 0.07$. The jagged line plots $\bar{x}(t)$ for 5,000 time units. As theory predicts, during the transition between peaks, \bar{x} moves from 0 to 1 as if the direction of natural selection were reversed, that is, at the same speed that \bar{x} moves by natural selection from 1 to 3.

that of the first part seems largely unknown.

Figure 1 is a computer simulation illustrating the theoretical results about equation (1). For comparison, Fig. 2 shows examples^{16,17} (from ref. 18) of observed punctuated equilibria with two different timescales.

In a changing landscape, punctuation can be triggered by selection, rather than drift, either by a rapid (for example, environmental) change¹⁹ or after a gradual change eliminates the currently occupied peak¹³. The introduction of a rare selectively superior mutant into a population from which it was previously absent can lead to punctuation^{20,21} corresponding to transition from an unstable equilibrium in a fixed landscape. Our analysis is the first to show that transitions between stable equilibria, triggered by drift in an unchanging adaptive landscape, should have fossil records indistinguishable from punctuations triggered by selection.

Gradual evolution is only possible in an unchanging landscape either if α is not small (violating neo-darwinian assumptions) or if sampling intervals are as short as the timescale of natural selection (unusual in fossil records). Even assuming many peaks, the suggestion^{20,22} that stepwise changes will appear to be gradual on a coarse timescale seems to be inconsistent with Wright's model: an increased timescale of observation implies⁵ that more local peaks are skipped over apparently instantaneously and stasis is observed only at higher fitness levels.

Gradual evolution is possible in a changing landscape if peaks shift gradually and unidirectionally. Our analysis suggests a resulting palaeontological pattern of 'punctuated shifting equilibria' as the gradual evolution of a population following a moving peak is punctuated by rapid transitions between peaks. It is unclear whether such changing landscapes should occur commonly.

Models similar to that described in equation (1) are applicable directly to populations that are panmictic or have much migration and hence are geographically homogeneous. Because the timescale τ_α is a rapidly increasing function of population size, equation (1) predicts stasis and punctuation for a small to moderate population but only stasis for a large population.

The model in equation (1) may be applied to an isolated subpopulation with a smaller τ_α than the larger parent population. Allopatric speciation will occur if the subpopulation, after

§ To whom correspondence should be addressed at the Rockefeller University.

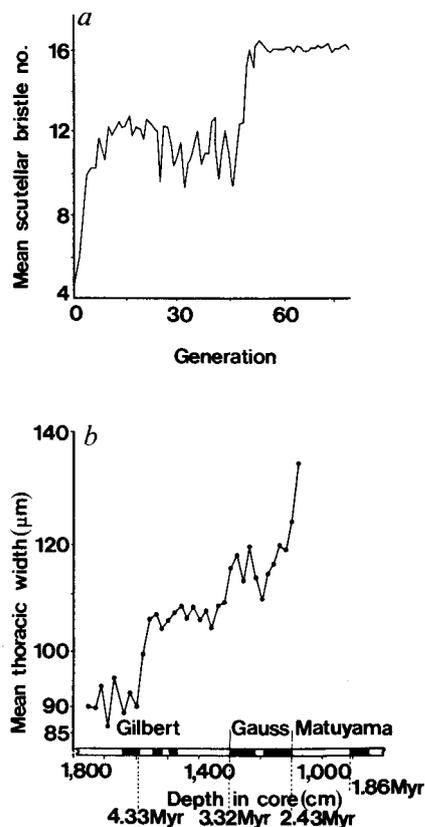


Fig. 2 a, Response to selection for scutellar bristle number in female *Drosophila* (presumably *melanogaster*; species not given¹⁶) according to MacBean *et al.*¹⁶, as simplified by Parsons¹⁸. b, Increase in thoracic width of the Antarctic radiolarian *Pseudocubus vema* during ~2.5 Myr according to Kellogg¹⁷, as simplified by Parsons¹⁸.

transition to a new peak, cannot interbreed with the parent population. Without requiring special 'genetic revolutions',²³ our analysis predicts that punctuated equilibria will be associated with the branching speciation of isolated subpopulations.

Generalizations of equation (1) incorporating spatial inhomogeneity in a local mean character correspond to Wright's

notion of local populations in his shifting balance model^{3,4}, in which he suggested that speciation could occur without physical barriers to migration and gene flow²³. Mathematically non-rigorous^{24,25} and rigorous²⁶ results suggest that punctuation occurs on the timescale τ needed to form by random drift (against natural selection) a 'critical droplet' (that is²³, a geographical region where transition to a higher peak of fitness occurs) which is of sufficient size to resist swamping by gene flow; such a critical droplet spreads rapidly by selection. The timescale τ is a slowly decreasing function of population size²⁷ (for fixed spatial density) because a critical droplet can form in each local subrange^{4,23}. Unlike τ_{cs} , this τ need not exceed geological timescales even for very large populations.

Our research was partially supported by USNSF grants MCS80-19384 (C.M.N.) and BSR84-07461 (J.E.C.), a Guggenheim Fellowship (C.M.N.), a MacArthur Fellowship (J.E.C.) and the hospitality of Mr and Mrs W. T. Golden (J.E.C.). We thank J. F. Crow, W. G. Faris, J. Felsenstein, L. R. Ginzburg, S. J. Gould, J. Maynard Smith, E. Mayr, W. M. Schaffer and L. S. Schulman for comments on earlier drafts.

Received 26 November 1984; accepted 12 March 1985.

1. Mayr, E. *Animal Species and Evolution* (Harvard University Press, 1963).
2. Lewontin, R. C. *The Genetic Basis of Evolutionary Change* (Columbia University Press, New York, 1974).
3. Wright, S. *Proc. 6th int. Congr. Genet.* Vol. 1, 356-366 (1932).
4. Wright, S. *Evolution and the Genetics of Populations* Vol. 3, 443-473; Vol. 4, 460-476 (University of Chicago Press, 1977, 1978).
5. Kipnis, C. & Newman, C. M. *SIAM J. appl. Math.* (in the press).
6. Eldredge, N. & Gould, S. J. in *Models in Paleobiology* (ed. Schopf, T. J. M.) 82-115 (Freeman, San Francisco, 1972).
7. Gould, S. J. & Eldredge, N. *Paleobiology* 3, 115-151 (1977).
8. Simpson, G. G. *Tempo and Mode in Evolution* (Columbia University Press, New York, 1944).
9. Simpson, G. G. *The Major Features of Evolution* (Columbia University Press, New York, 1953).
10. Hoffman, A. *Evol. Biol.* 15, 411-436 (1982).
11. Maynard Smith, J. *A. Rev. Genet.* 17, 11-25 (1983).
12. Geiger, G. *Math. Biosci.* 67, 59-79 (1983).
13. Kirkpatrick, M. *Am. Nat.* 119, 833-848 (1982).
14. Lande, R. *Evolution* 30, 314-334 (1976).
15. Galves, A., Olivieri, E. & Vares, M. E. *Ann. Probabil.* (submitted).
16. MacBean, I. T., McKenzie, J. A. & Parsons, P. A. *Theor. appl. Genet.* 41, 227-235 (1971).
17. Kellogg, D. E. *Paleobiology* 1, 359-370 (1975).
18. Parsons, P. A. *The Evolutionary Biology of Colonizing Species* (Cambridge University Press, 1983).
19. Wright, S. in *Genetics, Paleontology and Evolution* (eds Jepsen, G. L., Mayr, E. & Simpson, G. G.) 365-389 (Princeton University Press, 1949).
20. Ginzburg, L. *Paleobiology* 7, 426-429 (1981).
21. Petry, D. *Paleobiology* 8, 56-66 (1982).
22. Bookstein, F. L., Gingerich, P. D. & Kluge, A. G. *Paleobiology* 4, 120-134 (1978).
23. Barton, N. H. & Charlesworth, B. A. *Rev. Ecol. Systematics* 15, 133-164 (1984).
24. Fisher, M. E. *Physics* 3, 255-283 (1967).
25. Langer, J. S. *Ann. Phys.* 41, 108-157 (1967).
26. Faris, W. G. & Jona-Lasinio, G. *J. Phys.* A15, 3025-3055 (1982).
27. Newman, C. M. & Schulman, L. S. *J. statist. Phys.* 23, 131-148 (1980).